Elasticity Management of Streaming Data Analytics Flows on Clouds

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Abstract

A typical Streaming Data Analytics Flow (SDAF) consists of three layers: data ingestion, analytics, and storage, each of which is provided by a data processing platform. Despite numerous related studies, we still lack effective resource management techniques across an SDAF, leaving users struggling with a key question of: "What share of different resources (e.g. queue partitions, compute servers, NoSQL throughputs capacity) does each layer need to operate, given the budget constraints?". Moreover, unpredictability of streaming data arrival patterns coupled with different resource granularity across an SDAF leads to the following question: "How would we cope with the variable resource requirements across the layers for handling variation in volume and velocity of the streaming data flow?"

This paper introduces a framework that answers the above questions by employing advanced techniques in control and optimization theory. Specifically, we present a method for designing adaptive controllers tailored to the data ingestion, analytics, and storage layers that continuously detect and self-adapt to workload changes for meeting users’ service level objectives. Our experiments, based on a real-world SDAF, show that the proposed control scheme is able...
to reduce the deviation from desired utilization by up to 48% while improving throughput by up to 55% compared to fixed-gain and quasi-adaptive controllers. 

**Keywords:** Data analytics flow, Control theory, Data-intensive workloads, Resource management, Public clouds, Multi-objective optimization

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**1. Introduction**

Growing attention to data-driven enterprises and getting real-time insights into streaming data leads to the formation of many complex Streaming Data Analytics Flows (SDAF). For example, online retail companies need to analyse real-time click stream data and up-to-the minute inventory status for offering dynamically priced and customized product bundles. More importantly, cities are evolving into smart cities by fusing and analyzing data from several streaming sources in real-time. By analyzing data using streaming analytics flows, real-time situational awareness can be developed for handling events such as natural disasters, traffic congestion, or major traffic incidents.[1]

A cloud-hosted SDAF typically consists of three layers: data ingestion, analytics, and storage [2, 3]. The data ingestion layer accepts data from multiple sources such as online services or back-end system logs. The data analytics layer consists of many platforms including stream/batch processing systems, and scalable machine learning frameworks that ease implementation of data analytics use-cases such as collaborative filtering and sentiment analysis. The ingestion and analytics layers make use of different databases during execution and where required persist the data in the storage layer.

**1.1. Research Motivation and Challenges**

An SDAF is formed via orchestration [5] of different data processing platforms across a network of unlimited computing and storage resources. For example, Fig. [1] shows the Amazon reference SDAF [1] that performs real-time sliding-

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windows analysis over click stream data. In this architecture, Kinesis acts as a high-throughput distributed messaging system, Apache Storm\(^2\) as a distributed real-time computation system, and ElastiCache\(^3\) as a persistent storage.

Despite straightforward orchestration, elasticity management of the established flow has unique challenges (see 1.1) because it needs to cover three aspects: i) scalability, the ability to sustain workload fluctuations, ii) cost efficiency, acquiring only the required resources, iii) time efficiency, resources should be acquired and released as soon as possible\[6, 7, 8\].

Recent studies in elasticity management \[9\] lack a holistic view of the problem of resource requirements management (e.g. Compute servers, Cache nodes) of workloads, whereas \[10\] showed that the ability to scale down both web servers and cache tier leads to 65% saving of the peak operational cost, compared to 45% if we only consider resizing the web server tier. This leads us to the first research problem: How much resource capacity should be allocated to different big data platforms within an SDAF such that Service Level Objectives (SLO) are continuously met? There are two challenges in response to this question:

**Workload Dependencies.** In an SDAF, workloads pertaining to different platforms are dependent on each other, for example, changes in data velocity at the data ingestion layer lead to changes in CPU utilization at the data analytics layer. Fig. 2 clearly shows how the workload dynamics in the data injection layer can be traced down to the analytics layer, since the input records in inges-

\(^2\)http://storm.incubator.apache.org
\(^3\)http://aws.amazon.com/elasticache
Figure 2: The data arrival rate at the ingestion layer (Amazon Kinesis in Fig. 1) is strongly correlated (coefficient = 0.95) with the CPU load at the analytics layer (Apache Storm).

...tion layer strongly correlated with CPU usage in the analytics layer. To provide smooth elasticity management, these dependencies need to be detected dynamically. Existing approaches perform resource allocation across different layers irrespective of inter-layer workload dependencies which make them incapable of ensuring SLOs for emerging classes of SDAFs.

**Different Cloud Services and Monetary Schemes.** An SDAF is built upon multiple big data processing platforms and hardware resources offered by public clouds [11] [12] that adopt multiple pricing schemes [13]. For example, Amazon Kinesis\(^4\)\[^5\] pricing is based on two dimensions including shard hour\[^6\] and PUT Payload unit, whereas ElastiCache has one hourly pricing scheme which is based on the cache node type. To meet the SLOs (e.g. budget constraint) for a data analytics flow, resource requirements and their associated cost dimensions have to be considered during the allocation process.

Once the resource shares are determined, adaptive and timely provisioning of the resources is yet another issue which forms the second key research problem of this paper: *How can we sustain resource requirements of the SDAF in a timely...* 

\[^4\] http://aws.amazon.com/kinesis  
\[^5\] In Kinesis, a stream is composed of one or more shards, each provides a fixed unit of capacity.
In this regard, we face the following challenge:

**Uncertain Stream Arrival Patterns.** Variability of the streaming data arrival rates and their distribution models creates changing resource consumption in data stream processing workloads [14]. Moreover, forecasting data arrival patterns is challenging unless the data arrival rates follow some seasonal or periodical pattern. Therefore, we need an approach that can adjust to the changes very quickly while it keeps memory of elasticity decisions made from the near past.

### 1.2. Our Approach

To address the first research problem, an advanced technique from operations research is applied that helps in computing optimal resource allocation decisions in a principled and tractable fashion. To do so, we mathematically formulate the problem of finding the best resource shares across an analytics flow as a multiple criteria decision making problem in which optimal decisions need to be taken in the presence of trade-offs between multiple conflicting objectives.

In response to the second research problem, we use advanced control theoretic techniques. Previous studies [15, 16, 17, 18, 19, 20, 21] have shown clear benefits of using controllers in resource management problems against workload dynamics. However, we present the first attempt at applying adaptive controllers for elasticity management of multi-layered SDAF that integrates multiple big data processing platforms and cloud-based infrastructure services (e.g. VMs [22], provisioned read/write throughput of the tables). Our controller is equipped with the novel feature of having memory of recent controller decisions which leads to rapid elasticity [8] of the flow in response to workload dynamics.

### 1.3. Contributions

In summary, we make the following contributions:

- To the best of our knowledge, this is the first work that investigates the problem of multi-layered and holistic resource allocation of an SDAF deployed on public clouds. One of the core contributions of our work is
meticulous dependency analysis of the workloads along with the mathematical formulation of the problem as per the typical data ingestion, analytics, and storage layers of a data analytics flow (Section 3.2).

• We devise controllers individually tailored to the data ingestion, analytics, and storage layers that are able to continuously detect and self-adapt to time-varying workloads. A key contribution of the paper here is to propose a framework for design and asymptotic stability analysis of adaptive controllers by employing tools from classic nonlinear control theory. We also put forward the claim that this study is the first in automated control of SDAF on clouds (Sections 3.3 and 4).

• With numerous experiments on a real-world click-stream SDAF, we validate the efficiency of our techniques in elasticity management of a complex analytics flow under stringent SLO. We also show that, compared to the state of the art techniques, our approach is able to reduce the RMSE error (i.e. deviation from desired utilization) by up to 48% while increasing the throughput by up to 55% (Section 5).

1.4. Organization of the paper

The rest of the paper is organized as follows: related work is reviewed in the next section. Section 3.1 provides an overview of the proposed solution. Section 3.2 is devoted to the analysis of resource shares. In Section 3.3 we provide a generic adaptive elasticity control scheme and analyse its stability. Section 4 explains the design principles mandated by practical requirements of each layer of an SDAF, enabling effective employment of the proposed adaptive controller described in Section 3.3 along with the optimal resource allocation scheme outlined in Section 3.2 to design a complete SDAF resource management system. Experimental results are given in Section 5 and the concluding remarks in Section 6 complete the paper.
2. Related Work

This section describes the related work in two broad categories: stream data processing and elasticity management.

2.1. Stream Data Processing

Stonebraker et al. [23] outlined eight requirements of a real-time stream processing system such as guaranteeing data safety and availability, scaling applications automatically, processing and responding instantaneously, etc. that are somewhat supported by today’s stream processing systems. Having said that, emerging complex streaming data analytics flows which bring many platforms and technologies together entail revisiting and enhancing the features underpinning the requirements.

One of the key problems in streaming data analytics flows is to ensure end-to-end security as the medium of communication is untrusted. Nehme et al. [24] initially proposed the requirement of security in data stream environments, and they broadly divide the security issues into data-side and query-side security policies. The data-side security preferences are expressed via data security punctuations and the query-side access privileges are described by query security punctuations. The authors extensively work on access control by focusing on both query security punctuations in their papers [24, 25]. More recently, Puthal et al. [26, 27] proposed solutions i.e. Dynamic Prime Number Based Security Verification and Dynamic Key Length Based Security Framework, to protect big data streams from external and internal adversaries.

When it comes to scalability features, almost all of the recent stream processing systems have the capability to distribute processing across multiple processors and machines to achieve incremental scalability. However, adaptive and optimized provisioning of various cloud resources for different processing tasks across an SDAF has been neglected.
2.2. Elasticity Management

Elasticity and auto-scaling techniques have been studied extensively in recent years [9, 28]. Different techniques such as control theory [15], Queueing theory [29], fuzzy logic [30], Markov decision process [31] have been applied to tackle the problem with respect to different resource types such as Cache servers [32], HDFS storage [33], or VMs [34]. However, recent studies in resource management using control theory have clearly shown benefits of dynamic resource allocations against fluctuating workloads. More importantly, what makes the control theory approach stand out in workload management techniques is the fact that they do not rely on any prior information about the workload behavior and they impose very mild assumptions on the system model (e.g. as in queueing model). Such features lead to a simple yet effective approach that would sustain any workload’s shape and dynamics.

A number of inquiries [15, 33, 35, 36, 16, 17, 37, 18, 19, 20, 21] have been made into the elasticity management of either data-intensive systems or single/multi-tier web applications using control theory. Lama et al. in [16] propose a fuzzy controller for efficient server provisioning on multi-tier clusters which bounds the 90th-percentile response time of requests flowing through the multi-tier architecture. They further improve their approach in [17] by adding neural networks to the controller in order to avoid tuning the parameters on a manual trial-and-error basis, and come up with a more effective model in the face of highly dynamic workloads. Similar to this study, Jamshidi et al. in [35] propose a fuzzy controller that enables qualitative specification of elasticity rules for cloud-based software. They further equipped their technique in [36] with the Q-Learning technique, a model-free reinforcement learning strategy, to free users of most tuning parameters. More recently, Farokhi et al. in [37] use a fuzzy controller for vertical elasticity of both CPU and memory to meet the performance objective of an application.

In [33], the authors proposed a fixed-gain controller for elasticity management of a Hadoop Distributed File System (HDFS) [38] under dynamic web 2.0 workloads. To avoid oscillatory behavior of the controller, [33] develops a pro-
portional thresholding technique which in fact works by dynamically configuring the range for the controller variables. Similarly, in [18], the authors propose a multi-model controller which in fact integrates decisions from the empirical model and workload forecast model with the classical fixed-gain controller. The empirical model is to retrieve distinct configurations which are capable of sustaining the anticipated Quality of Service (QoS) based on recorded data from the past. In contrast, the forecast model which is built by Fourier Transformation is to provide proactive resource resizing decisions for specific classes of workloads.

More closely related to the topic of this paper, the authors in [20] propose a resource controller for multi-tier web applications. The proposed control system is built upon a black-box system modelling approach to alleviate the absence of first principle models for complex multi-tier enterprise applications. Unlike [20], the authors of [15] modeled the system (i.e. web server) as a second-order differential equation. However, the estimated system model used for control would become inaccurate if the real workload range were to deviate significantly from those used for developing the performance model. The authors of [20] next in [21] enhanced the previous work by employing multi-input multi-output (MIMO) control combined with a model estimator that captures the relationship between resource allocations and performance in order to assign the right amount of resource. The resource allocation system can then automatically adapt to workload changes in a shared virtualized infrastructure to achieve the average response time. Along similar lines, the authors in [19] incorporate a Kalman filter into a feedback controller to dynamically allocate CPU resources to virtual machines hosting server applications. However, our work differs in that our control system, rather than adjusting CPU allocation in a shared infrastructure, which commercial cloud providers do not provide, regulates resources in a higher abstraction level that is the number of instantiated VMs, for example. Above all, unlike our work, this class of control systems are only quasi-adaptive as their gain parameters do not rely on the history of the previously computed control gains and hence are unable to dynamically adapt.
to workload changes (see Section 3.3.2).

In summary, almost all of the above studies share the same constraint: lack of a holistic view on resource requirement management in which they have primarily investigated virtual server allocation problems even in a multi-tier Internet service. Our work completes this picture through studying different cloud resources including distributed messaging queue partitions (data ingestion layer), VMs (data analytics layer), and provisioned read or write throughputs of tables (data storage layer).

3. Proposed Solution

In this section we first provide an overview of the proposed solution and then we will discuss in detail its main components.

3.1. Solution Overview

Fig. 3 shows the main building blocks of our solution along with the architecture of our testbed which is a real-world SDAF - Click-Stream Analytics. Our testbed is similar to Amazon’s reference architecture as shown and discussed in Fig. 1 except ElasticCache is replaced with DynamoDB, a managed NoSQL database service, for seamless scalability. In this SDAF, Kinesis is used for managing the ingestion of streaming data (e.g. simulated URLs and referrers) at scale. Apache Storm processes streaming data and persists the aggregated counters (i.e. number of visitors) in DynamoDB. We discuss further the design principles followed in building our testbed in Section 4.

In a nutshell, the workflow of the solution is as follows: First, dependencies between workloads’ critical resource usage measures such as Kinesis shard utilization, Storm Cluster CPU usage, DynamoDB consumed read/write units are analysed. To this end, we apply linear regression techniques to the collected runtime and historical resource profiles to estimate the relationships among variables. The dependency information along with the cloud services costs and the user’s SLO (e.g. budget constraint) constitute the required inputs for the generation and then search of provisioning plan space.
The framework resource analyser is capable of determining the *maximum resource shares* of each layer in terms of the user’s budget constraint. Due to the multi-objective nature of the problem, there usually exist multiple feasible solutions; which one is best suited to the problem in practice must be identified either manually or randomly by the system.

Once the *upper bound* resource shares for each layer are identified, the adaptive controller tailored to each of the three layers automatically adjusts resource allocations of that layer. This means that the controllers can now freely operate within the limits of each layer resource. Note that the resource shares can be determined with respect to arbitrary time windows.

The controllers are regulated based on a number of parameters including monitored resource utilization value, desired resource utilization value, history of the controller’s decisions. In other words, the controllers continuously provision the resources to adequately serve the incoming records in order to keep resource utilization of each layer within the specified *desired value*. Note that for the sake of simplicity, the **sensor** and resource **actuator** as the key components of any controller-based elasticity management frameworks have not been depicted in Fig. 3. In our implementation the sensor module has been built on top of
CloudWatch and is responsible for providing recorded resource usage measures as per the specified monitoring window. The actuator is capable of executing the controllers’ commands such as adding/removing VMs, increasing/decreasing number of shards, and the like.

### 3.2. Resource Share Analysis

Having an efficient elasticity plan for an SDAF is challenging due to i) the diversity of cloud resources (e.g., number of Shards in Kinesis, number of VMs in Storm cluster) used to serve the flow, ii) different pricing schemes of cloud services, and iii) the dependency between workloads that altogether provide a complex provisioning plan space. This space can be of any shape in terms of SLOs, as such we formulate the goal as:

"Given the budget and estimated dependencies between workloads, what would be the maximum share of resources for each layer in a data analytics flow?"

**Problem Formulation:** The above problem in a general form is defined as a multi-objective (here three) function, since we aim at maximizing heterogeneous cloud resources and services in different layers across a flow. We use variables $r_{Tt}^{(L)}$ to represent the resource amount of type $T$ of the layer $L$ in a certain SDAF during time period $t$. Table I summarizes all parameters used for problem formulation of resource share analysis. Therefore,

\[
\arg\max \; \vec{r}_{Tt} = \left( r_{Iit}^{(I)}, r_{jit}^{(A)}, r_{kit}^{(S)} \right)
\]  

\footnote{https://aws.amazon.com/cloudwatch}
Table 1: List of key notations used in this paper.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
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<tbody>
<tr>
<td>$L = {I, A, S}$</td>
<td>$L$ set of the typical SDAF layers including Ingestion (I), Analytics (A), and Storage (S)</td>
</tr>
<tr>
<td>$T = {i, j, k}$</td>
<td>set of resources of types $i$, $j$, or $k$ (e.g. VMs, Queues).</td>
</tr>
<tr>
<td>$r^{(L)}_{Tt}$</td>
<td>resource amount of type $T$ of the layer $L$ in a certain streaming data analytics flow during time period $t$.</td>
</tr>
<tr>
<td>$c_{Td}$</td>
<td>cost of resource type $T$ of dimension $d$.</td>
</tr>
<tr>
<td>$Bud_t$</td>
<td>specified Budget at time $t$.</td>
</tr>
<tr>
<td>$Cap^{(L)}_{Tt}$</td>
<td>the capacity of resource type $T$ at layer $L$ at time $t$.</td>
</tr>
<tr>
<td>$a, b, c$</td>
<td>constant variables obtained via workload dependency analysis.</td>
</tr>
<tr>
<td>$u_k$</td>
<td>current actuator value. For example, in the analytics layer it represents the number of VMs allocated to a Storm cluster.</td>
</tr>
<tr>
<td>$u_{k+1}$</td>
<td>new actuator value. It actually represents the next step resource allocation amount.</td>
</tr>
<tr>
<td>$l_k$</td>
<td>the controller gain at time step $k$.</td>
</tr>
<tr>
<td>$y_k$</td>
<td>the current sensor measurement. For example, in the analytics layer it represents the CPU usage measured during the past monitoring window.</td>
</tr>
<tr>
<td>$y_r$</td>
<td>the desired reference sensor measurement (i.e. resource utilization) which is specified by the user.</td>
</tr>
<tr>
<td>$l_0, l_{max}, l_{min}$</td>
<td>respectively refer to initial, max, and min gain value.</td>
</tr>
<tr>
<td>$\gamma$</td>
<td>the controller parameter ($\gamma &gt; 0$).</td>
</tr>
</tbody>
</table>
subject to:

$$\sum_{i,d} r_{it}^{(I)} \cdot c_{id} + \sum_{j,d} r_{jt}^{(A)} \cdot c_{jd} + \sum_{k,d} r_{kt}^{(S)} \cdot c_{kd} \leq Bud_t$$ (2)

$$r_{it}^{(I)} = a \cdot r_{jt}^{(A)}$$ (3)
$$r_{it}^{(I)} = b \cdot r_{kt}^{(S)}$$ (4)
$$r_{jt}^{(A)} = e \cdot r_{kt}^{(S)}$$ (5)

$$\forall i, t : r_{it}^{(I)} \leq Cap_{it}^{(I)}$$ (6)
$$\forall j, t : r_{jt}^{(A)} \leq Cap_{jt}^{(A)}$$ (7)
$$\forall k, t : r_{kt}^{(S)} \leq Cap_{kt}^{(S)}$$ (8)
$$\forall i, j, k : r_{it}^{(I)}, r_{jt}^{(A)}, r_{kt}^{(S)} \in \mathbb{R}_+$$ (9)

$$i, j, k, d \in \mathbb{N}$$ (10)
$$a, b, e \in \mathbb{R}$$ (11)

where the resource shares of Ingestion (I), Analytics (A), and Storage (S) layers are positive real variables subject to the following constraints:

2 Budget Constraint: at every time period $t$ the sum of costs concerned with different cloud resources across all layers must be within the specified budget. Note that cloud services would have multiple cost dimensions $d$. For example, Kinesis pricing is based on two core dimensions – shard hour and PUT payload unit, and an optional dimension – Extended Data Retention. In contrast, the DynamoDB pricing model follows one dimension that is hourly rate based on the capacity you provision.

3 Dependency Constraints: dependency between layers in general would be any of the following forms: ingestion-to-analytics, ingestion-to-storage,

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[7] For the sake of simplicity, we assume that the cloud services base prices (e.g. $c_{id}$) remain unchanged during time periods. Moreover, to make the model more readable, we omit other miscellaneous expenses such as Data Transfer betweens layers.

[8] DynamoDB as an indexed datastore has another cost dimension - the disk space your data consumes, which is negligible in our application domain as the first 25 GB stored per month is free.
and analytics-to-storage. These models and in particular their constant variables including \( a, b, \) and \( e \) are learned and determined by the linear regression technique. Note that every flow would not necessarily exhibit all of these dependencies at a given point of time.

**Capacity Constraints:** at every time period \( t \) the calculated resource share must be within the cloud service capacity limits.

Subject to these constraints, we maximize different cloud resources across an SDAF. In multi-objective optimization, there does not typically exist a solution that minimizes or maximizes all objective functions simultaneously. Thus, attention is paid to Pareto optimal solutions; those that cannot be improved in any of the objectives without degrading at least one of the other objectives. This important concept is called domination. Put formally, in the context of our problem, a solution \( r_{1_{T,t}} \in \mathbb{R} \) is said to dominate another solution \( r_{2_{T,t}} \in \mathbb{R} \) if:

1. \( \forall T \in \{i, j, k\} \) and \( \forall L \in \{I, A, S\} : r_{1_{T,t}}^{(L)} \geq r_{2_{T,t}}^{(L)} \) and
2. \( \exists T \in \{i, j, k\} \) and \( \exists L \in \{I, A, S\} : r_{1_{T,t}}^{(L)} > r_{2_{T,t}}^{(L)} \)

Quite simply, this definition implies that \( r_{1_{T,t}} \) is Pareto optimal if there exists no feasible vector of decision variables \( r_{T,t} \in \mathbb{R} \) which would increase some criterion without causing a simultaneous decrease in at least one other criterion. Therefore, solving a multi-objective problem would not end up with a single solution, but rather a set of solutions called the Pareto front. We will discuss this in more detail in Section 5.2.

Having the maximum resource share of each layer would allow the controllers to operate within the limits of each layer freely. Moreover, it implicitly aims at maximizing an important QoS of the streaming workloads - Throughput, as it primarily depends on resource allocation.  

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There might be some limits in place for some cloud services. For example, provisioned throughput in DynamoDB has initial maximum of 40,000 write capacity units per table in a specific region, though one can request an increase on these limits.
3.3. Elasticity Controller

Control theory mandates that a system model that describes the mathematical relationship between the control input and output is specified before a controller is designed. Few studies in workload management of computer systems follow this approach in which the system is modelled, for example, as a difference equation [15] or using queueing theory. Due to the complexity and uncertainty of computer systems, obtaining dynamic models describing their behavior with difference equations requires implementation of comprehensive system identification techniques. These techniques inevitably increase the complexity of the control system and may decrease the robustness of the closed loop system (or even cause instability) if the system configuration or workload range deviates from those used to estimate the unknown system parameters. Similarly, in queueing theory every model is built upon a number of assumptions such as arrival process that may not be met by certain applications and workloads. Building and maintaining these models are complicated even for a multi-process server model [15], let alone a chain of diverse parallel distributed platforms, as we have in a complex data analytics flow.

For this reason, most prior work [33, 20, 21, 37, 35, 16, 17] on applying control theory to computer systems employs a black box approach in which the system model is assumed unknown and minimal assumptions are imposed on the system model that enable stability analysis of the closed-loop system. The downside of this approach is that it does not provide enough flexibility for proving strong stability results. In fact, most of the results available in the literature either lack proper stability analysis or only prove what is known as the internal stability (or at most bounded-input-bounded-output stability) in the control literature [39], implying that the resulting output error (i.e., the difference between the system output and its desired value) is bounded for all times. Nevertheless, it is known in the control literature that, in general, the internal stability does not imply asymptotic (or exponential) stability [39, 40], meaning that the output error is not only bounded, but also asymptotically (exponentially) converges to zero as time passes.
Therefore, here we propose a framework for designing controllers for computer systems and analyzing their stability by proposing a static, yet unknown, model for the underlying systems. Using this framework, we propose a generic adaptive controller which requires very minimal information about the system model parameters. Using tools from classic nonlinear control theory (e.g. Lyapunov theory), we provide a rigorous stability analysis and prove the asymptotic (exponential) stability of the resulting closed loop system [42].

3.3.1. A Framework for Controller Design and Stability Analysis

Denote the input of a system (assigned by the actuator) at the time $k$ by $u_k \in \mathbb{R}$ and the system output (i.e. the sensor reading) by $y_k \in \mathbb{R}$. We assume that the system input and output are related via a static, yet unknown, smooth function. That is to say $y_k = f(u_k)$ where $f : \mathbb{R} \rightarrow \mathbb{R}$ is a smooth function. In practice, the smooth function $f$ can be linearized at the operating point. Hence, we approximate the system model with a linear function (see Fig. 4a). Nevertheless, we still assume that the parameters of the linear model, i.e. the slope and the $y$-intercept, are unknown. That is,

$$y_k = au_k + b$$  (12)
with unknown $a \in \mathbb{R}$ and $b \in \mathbb{R}$. Note that, $a$ and $b$ generally depend on the operating point of the system (which itself depends on the workload). We further assume that an upper bound of the amplitude of $a$ and the sign of $a$ are known, that is, we know if the output is a decreasing ($a < 0$) or an increasing ($a > 0$) function of the input. These are very mild assumptions on the system model that can be easily verified in practice. For instance, increasing the number of virtual machines (i.e., the system input) in the data analytics layer decreases the CPU utilization (i.e., the system output or sensor reading$^{10}$). Hence, the corresponding system model for the data analytics layer is decreasing and $a < 0$ in this case.

Consider the control feedback loop illustrated in Fig. 4b. The control objective is to design the control input $u_k$ such that the output $y_k$ (remains bounded for all times and) converges to a reference (desired) constant value $y_r \in \mathbb{R}$ as $k$ goes to infinity.

For the sake of simplicity and without loss of generality, we assume $a < 0$ in the remaining parts of the paper. Nevertheless, the theory proposed here is applicable to the case that $a > 0$ with straightforward modifications.

### 3.3.2. A Generic Adaptive Controller

We propose the following adaptive controller.

$$u_{k+1} = u_k + l_{k+1}(y_k - y_r), \quad (13)$$

where the controller gain $l_{k+1}$ is adaptively updated according to the following multi criteria update law.

$$l_{k+1} = \begin{cases} l_k + \gamma(y_k - y_r), & \text{if } l_{\text{min}} \leq l_k + \gamma(y_k - y_r) \leq l_{\text{max}} \\ l_{\text{min}}, & \text{if } l_k + \gamma(y_k - y_r) < l_{\text{min}} \\ l_{\text{max}}, & \text{if } l_k + \gamma(y_k - y_r) > l_{\text{max}} \end{cases} \quad (14)$$

$^{10}$See Section 4.2 for further details on the data analytics layer controller
Here, \( l_k \) is the controller gain at the time \( k \), \( l_{\text{min}} > 0 \) and \( l_{\text{max}} > 0 \) are the lower bound and the upper bound of the controller gain\(^{11} \) respectively, and \( \gamma > 0 \) is a controller parameter. Table 1 summarizes all parameters used in the adaptive controller design.

The multi criteria update law \(^{14} \) ensures that the values of \( l_k \) are bounded by \( l_{\text{min}} \) and \( l_{\text{max}} \) for all \( k \) (the initial controller gain \( l_0 \) should be chosen such that \( l_{\text{min}} \leq l_0 \leq l_{\text{max}} \)). The proposed adaptive controller, the constant gain controller of \[^{33,18} \] and the quasi-adaptive controller of \[^{20} \] all have the same standard structure \[^{13} \]. The difference between these three control schemes is the gain \( l_{k+1} \). In the constant gain controller, the gain \( l_{k+1} \) is simply constant for all time. In the quasi-adaptive controller, the gain \( l_{k+1} \) is computed as a predetermined function of the measurements and desired output, however, this function is memoryless meaning that the gain \( l_{k+1} \) does not depend on \( l_k \) which is computed in the previous step. In contrast, the adaptive update rule \(^{14} \) does utilize the previously computed gain \( l_k \) for computing the new gain \( l_{k+1} \), thus resulting in a truly adaptive control scheme\[^{42} \].

In order to analyse the stability of the closed loop system, we define the output error

\[
e_k := y_k - y_r.
\] (15)

In ideal conditions where the measurements are noise free and the system model is accurate, the control goal is achieved if the error \( e_k \) converges to zero as \( k \) goes to infinity, yielding \( y_k \) to converge toward the desired output \( y_r \).

For stability analysis in the following theorem, we assume that \( a \) and \( b \) are constants (in theory). This assumption practically implies that the rate at which the control value \( u_k \) is computed is much faster than the speed at which the system parameters \( a \) and \( b \) change. This implies that the update rate of the controller should be much faster than the rate of change of the workload.

\(^{11}\)We later on propose criteria for choosing appropriate \( l_{\text{min}} \) and \( l_{\text{max}} \) to ensure stability of the closed loop system.
**Theorem 1.** Consider the system (12) and the controller (13) connected together according to Fig. 4b. Assume that $a$ and $b$ are constants, $a < 0$, and $0 < l_{\text{min}} \leq l_k \leq l_{\text{max}} < \frac{-2}{a}$ for all $k$. The controller ensures that the closed-loop system is globally exponentially stable. Moreover, defining $q(l_k) := 1 + (al_k)(2 + al_k)$ and $\alpha = -0.5 \ln(\max(q(l_{\text{min}}), q(l_{\text{max}}))) > 0$, we have $|e_k| \leq |e_0| \exp(-\alpha k)$ for all $k = 0, 1, 2, \ldots$ implying that $e_k$ exponentially converges to zero with a rate of convergence greater than $\alpha$. Moreover, the controller gain $l_k$ of the adaptive update rule (14) converges to a constant value for large enough $k$. $\blacksquare$

**Proof of theorem 1** Using (15) and (12) we have

\[ e_{k+1} = y_{k+1} - y_r = au_{k+1} + b - y_r. \]  

(16)

Replacing for $u_{k+1}$ from (13) into (16) and resorting to (12) yields

\[ e_{k+1} = a(u_k + l_k e_k) + b - y_r = a\left(\frac{1}{a}(y_k - b)\right) + l_k e_k + b - y_r = (1 + al_k)e_k. \]  

(17)

Equation (17) formulates the dynamics of the control error $e_k$. If the control gain $l_k$ is constant for all times, the error dynamics (17) represents a simple linear time-invariant (LTI) system whose stability could be analysed using linear control theory [43]. Nevertheless, in the general case where the control gain is time varying, we use Lyapunov theory from classic nonlinear control theory [39] [40] to analyse the stability of the error dynamics.

Consider the Lyapunov candidate

\[ V_k := e_k^2. \]  

(18)

Using (17), we have

\[ V_{k+1} - V_k = e_{k+1}^2 - e_k^2 = (1 + al_k)^2 e_k^2 - e_k^2 = (al_k)(2 + al_k)e_k^2 = (al_k)(2 + al_k)V_k. \]  

(19)

Assuming that $0 < l_k < \frac{-2}{a}$, we have $V_{k+1} - V_k \leq 0$ implying that the Lyapunov function is decreasing along the system trajectories and the closed-loop system is stable [39]. Defining $q(l_k) := 1 + (al_k)(2 + al_k)$ and using (19) we
have \( V_{k+1} = q(l_k)V_k \) which yields

\[
V_k = V_0 q(l_k)q(l_{k-1})\ldots q(l_1)q(l_0), \tag{20}
\]

for all \( k = 0, 1, 2, \ldots \). Since \( 0 < l_{\min} \leq l_k \leq l_{\max} < \frac{2}{a} \), it is straightforward to verify that \( 0 < q(l_k) \leq q_{\max} < 1 \) where \( q_{\max} := \max(q(l_{\min}), q(l_{\max})) \). Hence, we have \( q(l_k)q(l_{k-1})\ldots q(l_1)q(l_0) \leq q_{\max}^k \) which together with (20) yields

\[
V_k \leq V_0 q_{\max}^k = V_0 \exp(-\ln(q_{\max}^{-1})k), \tag{21}
\]

which implies that the geometric progression \( V_k \) decays exponentially to zero with a convergence rate greater than \( 2\alpha = \ln(q_{\max}^{-1}) > 0 \). Substituting for \( V_k \) from (21) into (18) and taking the square root of the sides we have

\[
|e_k| \leq |e_0|\exp(-\alpha k) \tag{22}
\]

which proves the first claim of the theorem.

Next, we proceed to show that the gain \( l_k \) converges to a constant value for large enough \( k \), say \( k = \infty \). We know that \( l_{\infty} \) is governed by one of the three criteria of the adaptation law (14). Suppose that \( l_k \) is governed by the first criteria for large \( k \). We use (15) to replace \( y_k - y_r \) with \( e_k \) in the first criteria of (14) to obtain \( l_{k+1} - l_k = \gamma e_k \). Taking the norm of the sides and recalling (22) we have \( |l_{k+1} - l_k| \leq \gamma |e_0|\exp(-\alpha k) \). Hence, for large enough \( k \) we have \( |l_{k+1} - l_k| \approx 0 \) which effectively implies that \( l_{k+1} \approx l_k \). This means that \( l_k \) converges to a constant value if \( l_k \) is governed by the first criteria for large enough \( k \). It remains to be shown that \( l_k \) converges to a constant value if it is not completely governed by the first criteria of (14). If \( l_{\infty} \) is governed by the second or the third criteria, we have either \( l_{\infty} = l_{\min} \) or \( l_{\infty} = l_{\max} \), respectively. Since \( l_{\min} \) and \( l_{\max} \) are both constants, \( l_{\infty} \) would be constant in this case as well. Note that, for large \( k \), \( l_k \) cannot indefinitely switch between the three criteria of (14) as we have already proved that \( l_k + \gamma(y_k - y_r) \), the value of which determines the criteria of (14), converges to a constant and eventually satisfies only one of the criteria for large \( k \). This completes the proof.
Remark 1. The stability proof of Theorem 1 is provided for a generic time-varying trajectory of control gain $l_k$. Hence, this stability proof is valid not only for the proposed adaptive update rule (14), but also for the constant gain controller (see e.g. [33]) and the quasi-adaptive controller [20] (provided that those controllers satisfy the gain requirements of theorem 1). For the case of the fixed gain controller, it can be verified that the requirements of theorem 1 are necessary and sufficient for exponential stability of the closed loop system.

In this case, theorem 1 provides coherent analytical limits on the gain of the controller that guarantee the stability of the closed loop system.

3.3.3. Gain Function ($l_k$) Behavior Analysis

One of the key indicators of an effective elasticity technique is the ability to quickly scale up or down, which is called the elasticity speed [8, 7]. The scale-up speed refers to the time it takes to shift from an under-provisioned state to an optimal or over-provisioned state. Conversely, the scale-down speed refers to the time it takes to shift from an over-provisioned state to an optimal or under-provisioned state [7].

We put forward the claim that our adaptive controller, compared to the fixed-gain controllers [33, 18] and quasi-adaptive controllers [20, 21], shows higher elasticity speed as it keeps the history of the controller decisions through updating the gain parameter with respect to the error (see Eq. 14). The bigger the gain-parameter value ($l_{k+1}$), the higher the speed of elasticity as per the standard controller Eq. (13) (also see Eq. (5) in [20] or Eq. (1) in [33]).

To support our claim, we first explain the normal and extreme scenarios of workload behaviors:

1. Normal overload/underload: In normal workload behavior, when a system is over-provisioned, de-scaling of resources leads to higher utilization ($y_k$) and hence decreases the distance from the desired value ($y_r$). Fig. 5a demonstrates this situation where the distance reduces from $|−80|$ (on the left) to the optimal point that is 0 (on the right). In contrast, when a system is under-provisioned, scaling of resources again reduces the error.
2. **Instantaneous massive overload/underload**: In contrast to normal work-load behavior, in the event of instantaneous massive overload or underload, scaling or de-scaling of the system does not necessarily decrease the error for a while. In other words, the system load increases or decreases much faster than the rate at which the resource manager reacts. Fig. 5c and 5d show this circumstance where in Fig. 5c the utilization is not improved (as we move from $|−80|$ to $|−100|$) even after de-scaling the resource. Similarly, scaling a highly overloaded system does not reduce the error $y_k - y_r$ and the distance increases from $|90|$ towards $|160|$ as shown in Fig. 5d. Note that this situation is temporary and the workloads will be back to a normal situation (Fig. 5a and 5b) sooner or later. Although transient, these extreme cases may typically either hit performance severely or lead to huge resource wastages.

Now we can look into the gain parameter behavior in different scenarios and compare the elasticity speed of different controllers as shown in Fig. 5. The gain function of our controller $l_{k+1} = l_k + \gamma(y_k - y_r)$ is shown with the
green line with circle marker alongside the fixed-gain function \( l_{k+1} = l_k \) (the blue line with square marker) and quasi-adaptive gain function \( l_{k+1} = ((1/y_r) - \epsilon) * (y_k/y_r) \) (the purple line with asterisk marker).

As the figures show, our gain function produces the higher value in all scenarios, which in turn leads to a higher elasticity speed. The only exception to this observation is Fig. 5a where a fixed-gain controller generates the higher value. However, we have witnessed in numerous experiments that even in this situation our controller performs faster. This scenario does not happen in isolation and a typical workload experiences all of the scenarios in its lifetime, so that the gain parameter in its initial stage has a larger value. For example, suppose that the workload firstly goes through one of the situations depicted in Fig. 5b, 5c, or 5d and then 5a. Clearly, after passing one of these situations the value of \( l_{k+1} \) is bigger (here respectively is \( > 0.08 \), \( > 0.15 \), or \( > 0.15 \)) than the initial value of a fixed-gain controller in 5a that is 0.05. Therefore, these numbers simply means that our controller has higher elasticity speed, compared to its competitors. We will discuss the advantages of this capability in more detail in Section 5.3.

4. Automated Control of an SDAF

The cloud services and resources in different layers of an SDAF are of different granularity levels (e.g. a VM in the analytics layer cluster as opposed to the read/write unit in the storage layer) and are sometimes restricted to specific limitations (e.g. de-scaling operations limit in DynamoDB ). Therefore, each layer mandates a set of specific design principles for its controller. Therefore, this section discusses how the proposed controller associated with each layer works and explains the principles used in the design in terms of the real world click-stream SDAF.

4.1. Data Ingestion Layer Controller

Our controller in the data ingestion layer is responsible for resizing of the Kinesis cloud service. A data stream in Kinesis is composed of one or more
shards, each of which provides a fixed unit of capacity\(^{12}\) for persisting incoming records. Therefore, the data capacity of the stream is a function of the number of shards that are specified for the stream. As the data rate increases, more shards need to be added to scale up the size of the stream. In contrast, shards can be removed as the data rate decreases.

As mentioned in Section 3.1, each controller is equipped with both sensor and actuator components. The sensor here continuously reads the incoming records stream from CloudWatch and calculates the resource utilization as average write per second:

\[
\frac{\left(\sum_{i=1}^{n} \text{IncomingRecords}_i\right)}{\left(n \times 60\right)} \div \left(\text{ShardsCount} \times 1000\right)
\]

where \(n\) is the number of monitoring time windows in minutes and assuming each record is less than 1 KB. This measure inputs the controller and it then makes the next resource resizing decision as per the logic discussed in Section 3.3.1 and invokes the actuator to execute increaseShards, decreaseShards, or doNothing commands.

4.2. Data Analytics Layer Controller

The analytics layer controller in the click-stream application is in charge of Apache Storm cluster resizing. A Storm cluster consists of the master node and the worker nodes which are coordinated by Apache ZooKeeper. The master node is responsible for distributing code around the cluster, assigning tasks to workers, and monitoring for failures. Each worker node listens for work assigned to its machine and starts and stops worker processes as necessary based on what a master has assigned to it. Each worker process executes a subset of a job called topology; a running topology consists of many worker processes spread across many machines. The logic for a realtime application is packaged into a Storm topology, a graph of stream transformations.

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\(^{12}\)Each shard supports up to 5 transactions/second for reads, up to a maximum total data read rate of 2 MB/second and up to 1,000 records/second for writes, up to a maximum total data write rate of 1 MB/second.
Our Storm cluster is built on the Amazon EC2 instances whose size is regulated by the control system. The sensor here records the CPU utilization of the cluster in terms of the specified time window. Following that the instances are acquired or released. However, this process is not instant and it may take several minutes to start up a VM. During this time, the data flow analytics is vulnerable to missing the SLOs. In response and to counter this problem, we inject a number of already configured worker VMs in the cluster under Stopped status. In the event of scaling, these pre-configured VMs are added to the cluster at the earliest opportunity.

To release a worker VM in the event of de-scaling, our actuator finds the most economical VM to stop. The EC2 instance prices are on an hourly basis. As the instances are fired in different time slots, it is more economical to stop the instance that uses the maximum of its current time slot. Therefore, the instance that has the least remaining time of the current paid 1 hour slot is the economical candidate to be stopped. Fig. 6 shows a sample of three VMs with different uptimes and remaining times where VM 2 and then 1 are respectively the most economical VMs to be stopped. We calculate those instances that show least cost to stop using the following equation:

\[
\min_{i \in n} f(vm_i),
\]

\[
f(vm_i) = \text{uptime}_{vm_i} \mod t
\]

where \text{uptime} refers to the VM uptime and \( t \) is the time slot which is on an hourly basis in AWS.\(^{13}\)

4.3. Data Storage Layer Controller

DynamoDB sits in our storage layer and is capable of persisting the analytics results. The controller in this layer is responsible for adjusting the number of provisioned write capacity units where each unit can handle 1 write per

\(^{13}\)In our experiments, the \text{uptime} is retrieved from CloudWatch in milliseconds, and hence the \( t \) is set to the value of 1h * 60min * 60sec * 1000millsec.
second. To this end, the sensor retrieves the ConsumedWriteCapacityUnits from CloudWatch and calculates write utilization per second as a main input to the control system as follows:

\[
\frac{\left(\sum_{i=1}^{n} \text{ConsumedWriteCapacityUnits}\right)}{\text{ProvisionedWriteCapacityUnits}(n \times 60)}
\]

where \( n \) is the number of monitoring time windows in minutes and assuming items are less than 1 KB in size. This measure inputs the controller and following that the next resource resizing decision is made and the actuator is invoked to execute increaseProvisionedWriteCapacity, decreaseProvisionedWriteCapacity, or doNothing commands.

Cloud services sometimes come with some limitations in the number of scaling or de-scaling operations in a certain period of time. For example, in DynamoDB a user can not decrease the ReadCapacityUnits/WriteCapacityUnits settings more than four times per table in a single UTC calendar day. This limitation may lead to reasonably high resource waste in highly fluctuating workloads. To address this issue, our controller uses a simple yet effective back-off strategy. The actuator performs the de-scaling operation only after reaching the back-off threshold - a number of consecutive de-scaling requests from the controller. This strategy filters transient behavior of workloads and alleviate the problem of resource waste.
5. Experimental Results

The purpose of our experiments in this section is to demonstrate that (i) given the budget and dependency constraints, we are able to efficiently determine the share of different resources across an SDAF (Section 5.2), (ii) Our controller outperforms the state of the art fixed-gain and quasi-adaptive controllers in managing fine-grained cloud resources in dynamic data stream processing settings (Section 5.3), and most importantly (iii) our framework is able to manage elasticity of the SDAF on public clouds (Section 5.4).

5.1. Experimental Setup

We have implemented our framework in Java. To implement the workload dependency and resource share analyser, we respectively employed Apache Commons\(^{14}\) and the MOEA framework \(^{44}\). We tested our controllers and resource share analyser against real world click-stream analytics, as shown in Fig. 3.

In the testbed, we used three t2.micro instances as click-stream data producers\(^{15}\), each is able to produce up to \(\sim 5K\) records per seconds. The data ingestion and storage, as discussed earlier, are handled by Amazon Kinesis and DynamoDB services. The Storm cluster is made up of two m4.large instances for Zookeeper and Storm master node (i.e. Nimbus server in Storm terminology) and a number of workers (i.e. supervisors) which are either t2.micro, t2.small, m3.medium, or m4.xlarge.

5.2. Evaluation Results: Optimized Resource Share Determination

To solve a multi-objective optimization problem and find the Pareto front, a large number of algorithms exist in the literature \(^{11}\). Our framework uses a nondominated sorting genetic algorithm II (NSGA-II) \(^{45}\) to search the provisioning plan space.

\(^{14}\)http://commons.apache.org
\(^{15}\)https://github.com/awslabs/amazon-kinesis-data-visualization-sample
The prerequisite of resource share determination is workload dependency analysis. To illustrate how the framework computes with the resource shares of each layer, in our testbed the following constraints were evaluated:

1. $5 \times r_{j_{t1}}^{(A)} \geq r_{i_{t1}}^{(I)}$
2. $2 \times r_{j_{t1}}^{(A)} \leq r_{i_{t1}}^{(I)}$
3. $2 \times r_{i_{t1}}^{(I)} \leq r_{k_{t1}}^{(S)}$

where $i$, $j$, and $k$ respectively refer to the number of shards in ingestion, VMs in analytics, and Write Capacity units in storage layer at time $t1$. Moreover, suppose that the daily budget of running the click-stream analytics flow on public clouds is $32.25. Given the budget and dependency constraints formulated in Section 3.2, the algorithm finds the Pareto optimal solutions and its corresponding frontier surface as displayed in Fig. 7a and 7b.

As we can see, solving the problem ends up with six feasible solutions (see Fig. 7a), each representing the resource shares of Kinesis, Storm, DynamoDB simultaneously. The underlying assumption here is that a solution to the problem must be identified by an expert to be implemented in practice. For example, the DevOps manager of the analytics flow plays an important role as it is expected to be an expert in the problem domain.

5.3. Evaluation Results: Adaptive Controller Performance

In this section, we report the performance of our controller, compared with the state of the art constant gain $^{33,18}$ and quasi-adaptive controllers $^{20}$. Due to workload fluctuations over time, it is hardly possible to provide a truly-fair testbed for comparison. Having said that, we modified the testbed to make it as fair as possible for pair-wise comparison between controllers. To this end, we conducted the experiments on all layers but analytics, since it is hard to control the input to this layer. In other words, as the inputs to Kinesis and DynamoDB are manageable, we could provide a fair starting point for the systems.

Fig. 8a and 8b denote the architecture of the Kinesis and DynamoDB controllers testbed. In the former, we have created three streams in Amazon Kinesis.
with the same configurations and settings (e.g., No. of shards, region). The data
generator puts the same click-stream data to the streams. In the latter, we have
created three equivalent tables in which three copies of the results are written
by the application running on a Storm cluster. Note that in both cases, even
though the data are nearly sent at the same rate at the beginning, different
resource resizing decisions lead to different capacity, and hence the workload
inevitably becomes a different shape.

**Performance Evaluation Metric.** To evaluate and compare the perform-
ance of controllers, we use root mean squared error (RMSE) of desired resource
utilization:

\[
\sqrt{\frac{\sum_{k=1}^{n} (y_k - y_r)^2}{n}}
\]  

(26)

where \(y_k\) and \(y_r\) are respectively the measured resource usage at time \(k\) and
the desired resource utilization (i.e., reference resource usage). The \(n\) variable
also refers to the number of samples. Note that this measure basically captures
the deviation from desired utilization. Intuitively, the well-performed controller
shows the least deviation.

To compare our work with the state of the art, five runs were conducted for
(a) Kinesis controllers testbed  
(b) DynamoDB controllers testbed

Figure 8: a) The data producer puts the same records to the three identical Kinesis streams, regulated by the controllers.  
b) Our implementation writes three copies of the results to the three identical DynamoDB tables.

(a) RMSE of Kinesis workload  
(b) RMSE of DynamoDB workload

Figure 9: The RMSE measures for both a) Kinesis and b) DynamoDB workloads in terms of different desired utilization ($y_r$) values.

Each workload (i.e. Kinesis and DynamoDB) under different desired utilization values ($y_r$): 50%, 60%, 70%, 80%, and 90%. Each run in Kinesis took approximately 4 hours (i.e. 85 samples every 3 minutes). The time period was less than 2 hours (i.e. 60 samples for every 2 minutes) in DynamoDB due to the discussed service limitation.

Fig. 9a shows the results of these runs in Kinesis in which our proposed controller outperforms the competing controllers in all runs but one, $y_r = 90\%$. Fig. 10 displays the throughput, incoming records per second to Kinesis, recorded during the experiments. As you can see, the adaptive controller in all runs ei-
ther produces comparable throughput (i.e. when $y_r = 50\%$ or $y_r = 70\%$) or improves it considerably by up to 55\% when $y_r = 60\%$.

In the DynamoDB workload, our controller with adaptive gain produces less error (RMSE) than the quasi-adaptive controller in all but one run when $y_r = 60\%$. When it comes to comparison with the constant gain controller, the adaptive control system is less successful as it shows higher error rates in 3 out of 5 runs (i.e. $y_r = 50\%, 60\%, \text{ and } 90\%$). This is mainly due to the DynamoDB de-scaling limitation (as discussed in Section 4.3). The adaptive controller essentially adjusts the gain parameter with respect to the workload dynamics, whereas the service does not allow more than four de-scaling operations in a day. To handle that we devised the back-off strategy (see Section 4.3) which even though it alleviates the problem, hinders the optimal functioning of the control system.

To provide a clear picture of the point as well as how the controller functions in each run, consider Fig. 11 and 12 which respectively depict two sample runs of Kinesis and DynamoDB. As you can see, the controllers in Kinesis workloads perform better compared with the DynamoDB, since they face no restriction in executing scaling/de-scaling commands. In other words, the adaptive and quasi-adaptive controllers could not react to the dynamics of DynamoDB workloads.
so that they perform worse than the fixed-gain controller whose gain function is independent of the workload changes.

In summary, our control system outperforms the quasi-adaptive and fixed-gain controllers respectively in 80% (8 out of 10) and 60% (6 out of 10) of runs conducted based on two different cloud services using a click-stream analytics flow workload. This finding is based on the fact that our control system has a higher elasticity speed as illustrated in 3.3.3 which in turn reduces the error, the deviation from the desired resource utilization value.

5.4. Evaluation Results: Automated Control of the Flow

In this section, we discuss the adaptive controller’s performance in elasticity management of the click-stream analytics flow. Fig. 13 shows how the tailored adaptive controllers to the data ingestion, analytics, and storage layers function against real dynamic workload. In the data ingestion layer the control system properly responds to the incoming record workload and increases/decreases the number of shards accordingly in order to keep the utilization (see Eq. 23) within the desired threshold i.e. $y_r = 60\%$. 

Figure 11: Performance comparison of our adaptive controller and the fixed-gain and quasi-adaptive ones in Amazon Kinesis workload management with $y_r = 70\%$. 

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33
Figure 12: Performance comparison of our adaptive controllers and the fixed-gain and quasi-adaptive ones in DynamoDB workload management with $y_r = 60\%$.

Figure 13: Adaptive controller’s performance in elasticity management of a) data ingestion ($y_r = 60\%$), b) analytics ($y_r = 40\%$), c) and storage ($y_r = 70\%$) layers of the click-stream analytics flow with $l_k = 0.03$ and $\gamma = 0.0001$. 

34
Workload management of the Storm analytics cluster is shown in Fig. 13b, in which the controller increases the size of the cluster when CPU usage grows from around 34% to 67% at the 47th sample point. As you can see, after scaling the CPU utilization reduces, however its distance from the target utilization value (40%) is not big enough to cause de-scaling of the cluster.

When it comes to the data storage layer (Fig. 13c), the adaptive control system successfully replies to the workload fluctuations. Having said that, the experiment was conducted while the back-off functionality of the controller was on and set to the value of 2. It means that the de-scaling command would be executed when we encounter multiple requests for de-scaling in a consecutive manner. For example, at the 10th sample point the provisioned write capacity units reduce from 7 to 6. In a similar observation, from the 16th to the 25th sample points the capacity diminishes from 8 to 3 units. In contrast, from the 25th onward up to the 92nd sample point, the write units enlarge to 8 units.

In summary, our proposed adaptive control system is able to manage elasticity of the streaming data analytics flow on public clouds. Although we have implemented and tailored the framework for the click-stream analytics flow, our approach does not hold any hard assumptions about the specifics of the application and the underlying data-intensive systems. Therefore, it can be employed for the other SDAFs which may be served by different data-intensive platforms (e.g. Apache Kafka\textsuperscript{16}, Apache Spark\textsuperscript{17} and the like).

6. Conclusions and Future Work

Elasticity management of the streaming big data analytics flow has a number of unique challenges: workload dependencies, different cloud services and monetary schemes, and uncertain stream arrival patterns. To address the first two challenges, we formulated the problem of resource share analysis across the analytics flow using a multi-objective optimization technique. The experiments

\textsuperscript{16}http://kafka.apache.org
\textsuperscript{17}http://spark.apache.org
showed that the proposed technique is able to efficiently determine resource shares with respect to various constraints.

We then presented three adaptive controls for data ingestion, analytics, and storage layers in response to the last challenge. Apart from theoretically proving exponential stability of the control system, numerous experiments were conducted on the click-stream SDAF. The results showed that compared with the quasi-adaptive and fixed-gain controllers, our control system respectively reduces the deviation from desired utilization in 80% and 60% of runs while improving the QoS.

For future work, we plan to extend the system functionalities to be able to i) analyze the cloud resource costs per analytics flows, and ii) to visualize end-to-end QoS of the SDAFs with drill-down features in order to diagnose performance issues in the complex flows, iii) extending the framework for controller design and analysis enabling application of more advanced control techniques such as robust or robust-adaptive controller design.

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